CSE 258 — Lecture 7 Web Mining and Recommender Systems

Recommender Systems

The goal of recommender systems is...To help people discover new content

Recommendations for You in Amazon Instant Video See more















The goal of recommender systems is... To help us find the content we were already looking for



By placing your order, you agree to our Terms of Use. Sold by Amazon Digital Services, In

Customers Who Watched This Item Also Watched



The goal of recommender systems is... To discover which things go together



Calvin Klein Men's Relaxed Straight Leg Jean In Cove *** * * * 20 customer reviews Price: \$48,16 - \$69,99 & FREE Returns, Details Select Sizing info | Fit: As expected (55%) Color: Cove 98% Cotton/2% Elastane Imported Button closure Machine Wash · Relaxed straight-leg jean in light-tone denim featuring whiskering and five-pocket styling · Zip fly with button · 10.25-inch front rise, 19-inch knee, 17.5-inch leg opening Frequently Bought Together Calvin Klein Jeans Calvin Klein Jeans \$57.94 - \$69.50 \$50.67 - \$60.00 \$22.00 - \$68.00

Page

Customers Who Bought This Item Also Bought



The goal of recommender systems is...
To personalize user experiences in response to user feedback

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The goal of recommender systems is...

• To recommend incredible products that are relevant to our interests



The goal of recommender systems is...To identify things that we **like**

Results for 'mad max'	Mad Max 1979 R 93 minutes	
Ma (15 In	In a postapocalyptic future, jaded motorcycle cop Max Rockatansky is ready to retire. But his world is shattered when a malicious gang murders his family as an act of retaliation, forcing a devastated Max to hit the open road seeking vengeance.	100 million (100 m
tou	Starring: Mel Gibson, Hugh Keays-Byrne	
vic	Director: George Miller	1
N I N Y	Genre: Sci-Fi & Fantasy	
Ge	Format: DVD	
Add Th		
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The goal of recommender systems is...

- To help people discover new content
- To help us find the content of e were To model people's
- To dis preferences, opinions, bgether
 To p and behavior ces in
 - To p and behavior ces in
 - To identify things that we **like**

Suppose we want to build a movie recommender

e.g. which of these films will I rate highest?



We already have a few tools in our "supervised learning" toolbox that may help us

Pitch Black - U	nrated Director	S Cut R CC
ATCH BLACK	When their ship crash-lar escaped convict Riddick lurk in the shadows, wait See More Starring: Vin Diesel, Radh Runtime: 1 hour, 53 minut Available to watch on su	The 7.1/10 adds on a remote planet, the marooned passengers soon learn that (Vin Die el) isn't the only thing they have to fear. Deadly creatures ing to atta k in the dark, and the planet is rapidly plunging into the a Mitchell es poported device s.
UNRATED	Product Details	
A. Phillips	Product Details	Science Fiction Horror
UNRATED A. Phillips Reviewer ranking: #17,230,554	Product Details Genres	Science Fictic - Action, Horror
A. Phillips Reviewer ranking: #17,230,554 90% helpful	Product Details Genres Director	Science Fictio, Action, Horror David Twohy Vin Diesel, Badis Mitchell
UNRATED A. Phillips Reviewer ranking: #17,230,554 90% helpful votes received on reviews (151 of 167)	Product Details Genres Director Starring Supporting actors	Science Fictic Action, Horror David Twohy Vin Diesel, Radh, Mitchell Cole Hauser, Keith David, Lewis Fitz-Gerald, Claudia Black, Rhiana Gr Angela Moore, Pet, Chiang, Ken Twohy
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UNRATED A. Phillips Reviewer ranking: #17,230,554 90% helpful votes received on reviews (151 of 167) ABOUT ME Enjoy the reviews ACTIVITIES Reviews (16) Public Wish List (2) Listenzini List (2)	Product Details Genres Director Starring Supporting actors Studio MPA1 rating O ptions and subtitles Rental rights Purchase rights	Science Fictic Action, Horror David Twohy Vin Diesel, Radhi Mitchell Cole Hauser, Keith David, Lewis Fitz-Gerald, Claudia Black, Rhiana Gr Angela Moore, Petri Chiang, Ken Twohy NBC Universal R (Restricted) English Details * 24 hour viewing period. Et tails * Stream instantly and down, ad to 2 locations Details *

 $f(\text{user features, movie features}) \xrightarrow{?} \text{star rating}$

$f(\text{user features, movie features}) \xrightarrow{?} \text{star rating}$

Movie features: genre, actors, rating, length, etc.

Product Details

Genres	Science Fiction, Action, Horror	
Director	David Twohy	
Starring	Vin Diesel, Radha Mitchell	
Supporting actors	Cole Hauser, Keith David, Lewis Fitz-Gerald, Claudia Black, Rhiana Gr Angela Moore, Peter Chiang, Ken Twohy	
Studio	NBC Universal	
MPAA rating	R (Restricted)	
Captions and subtitles	English Details 🔻	
Rental rights	24 hour viewing period. Details 💌	
Purchase rights	Stream instantly and download to 2 locations Details 💌	
Format Amazon Instant Video (streaming online video and digital downlo		

User features: age, gender, location, etc.

A. Phillips

Reviewer ranking: #17,230,554

90% helpful votes received on reviews (151 of 167)

ABOUT ME Enjoy the reviews...

ACTIVITIES Reviews (16) Public Wish List (2) Listmania Lists (2) Tagged Items (1)

 $f(\text{user features}, \text{movie features}) \xrightarrow{?} \text{star rating}$

With the models we've seen so far, we can build predictors that account for...

- Do women give higher ratings than men?
- Do Americans give higher ratings than Australians?
- Do people give higher ratings to action movies?
- Are ratings higher in the summer or winter?
- Do people give high ratings to movies with Vin Diesel?

So what **can't** we do yet?

 $f(\text{user features}, \text{movie features}) \xrightarrow{?} \text{star rating}$

Consider the following linear predictor (e.g. from week 1):

$$\begin{split} f(\text{user features}, \text{movie features}) = \\ \langle \phi(\text{user features}); \phi(\text{movie features}), \theta \rangle \end{split}$$

But this is essentially just two separate predictors!

f(user features, movie features) =

 $= \langle \phi(\text{user features}), \theta_{\text{user}} \rangle + \langle \phi(\text{movie features}), \theta_{\text{movie}} \rangle$

user predictor

movie predictor

That is, we're treating user and movie features as though they're **independent!**

But these predictors should (obviously?) **not** be independent

f(user features, movie features) = f(user) + f(movie)

do I tend to give high ratings?

does the population tend to give high ratings to this genre of movie?

But what about a feature like "do I give high ratings to **this genre** of movie"?

Recommender Systems go beyond the methods we've seen so far by trying to model the **relationships** between people and the items they're evaluating





Recommender SystemsCollaborative filtering

(performs recommendation in terms of user/user and item/item similarity)

2. Assignment 1

3. (next lecture) Latent-factor models

(performs recommendation by projecting users and items into some low-dimensional space)

4. (next lecture) The Netflix Prize

Defining similarity between users & items

Q: How can we measure the similarity between two users?
A: In terms of the items they purchased!

Q: How can we measure the similarity between two **items?**

A: In terms of the users who purchased them!

Defining similarity between users & items

e.g.: Amazon



Calvin Klein Men's Relaxed Straight Leg Jean In Cove

**** * 20 customer reviews

Price: \$48.16 - \$69.99 & FREE Returns. Details Size Select Sizing info | Fit: As expected (55%) * Color: Cove · 98% Cotton/2% Elastane - Imported Button closure Machine Wash · Relaxed straight-leg jean in light-tone denim featuring whiskering and five-pocket styling · Zip fly with button 10.25-inch front rise, 19-inch knee, 17.5-inch leg opening Frequently Bought Together

Calvin Klein Jeans

\$49.92





Levi's \$23.99 - \$68.00







Customers Who Viewed This Item Also Viewed

Customers Who Bought This Item Also Bought









Calvin Klein Jeans

\$57.94 - \$69.50



















Definitions

Definitions

 I_u = set of items purchased by user u U_i = set of users who purchased item i

Definitions



 R_u = binary representation of items purchased by u $R_{.,i}$ = binary representation of users who purchased i

$$I_u = \qquad \qquad U_i =$$

0. Euclidean distance

Euclidean distance:

e.g. between two items i,j (similarly defined between two users)

$$|U_i \setminus U_j| + |U_j \setminus U_j| = ||R_i - R_j||$$

0. Euclidean distance

Euclidean distance:

e.g.: $U_1 = \{1,4,8,9,11,23,25,34\}$ $U_2 = \{1,4,6,8,9,11,23,25,34,35,38\}$ $U_3 = \{4\}$ $U_4 = \{5\}$

$|U_1 \setminus U_2| + |U_2 \setminus U_1| = |U_3 \setminus U_4| + |U_3 \setminus U_4| =$

Problem: favors small sets, even if they have few elements in common

1. Jaccard similarity

$\operatorname{Jaccard}(A, B) =$

$\operatorname{Jaccard}(U_i, U_j) =$

→ Maximum of 1 if the two users purchased **exactly the same** set of items (or if two items were purchased by the same set of users)

→ Minimum of 0 if the two users purchased completely disjoint sets of items (or if the two items were purchased by completely disjoint sets of users)

2. Cosine similarity



 $\cos(\theta) = 1$

(theta = 0) \rightarrow A and B point in exactly the same direction

 $\cos(\theta) = -1$ (theta = 180) \rightarrow A and B point in opposite directions (won't actually happen for 0/1 vectors)

 $\cos(\theta) = 0$ (theta = 90) \rightarrow A and B are orthogonal

2. Cosine similarity

Why cosine?

- Unlike Jaccard, works for arbitrary vectors
- E.g. what if we have **opinions** in addition to purchases?



2. Cosine similarity

E.g. our previous example, now with "thumbs-up/thumbs-down" ratings

Uharry potter — (vector representation of users' **ratings of** Harry Potter)



 $\cos(\theta) = 1$

(theta = 0) \rightarrow Rated by the same users, and they all agree

 $\cos(\theta) = -1$ (theta = 180) \rightarrow Rated by the same users, but they **completely disagree** about it

> $\cos(\theta) = 0$ (theta = 90) \rightarrow Rated by different sets of users

What if we have numerical ratings (rather than just thumbs-up/down)?



What if we have numerical ratings (rather than just thumbs-up/down)?

What if we have numerical ratings (rather than just thumbs-up/down)?

- We wouldn't want 1-star ratings to be parallel to 5star ratings
 - So we can subtract the average values are then negative for below-average ratings and positive for above-average ratings

$$\operatorname{Sim}(u,v) = \frac{\sum_{i \in I_u \cap I_v} (R_{u,i} - \bar{R_u})(R_{v,i} - \bar{R_v})}{\sqrt{\sum_{i \in I_u \cap I_v} (R_{u,i} - \bar{R_u})^2 \sum_{i \in I_u \cap I_v} (R_{v,i} - \bar{R_v})^2}}$$

Compare to the cosine similarity:

Pearson similarity (between users):

items rated by both users average rating by user v

$$\operatorname{Sim}(u,v) = \frac{\sum_{i \in I_u \cap I_v} (R_{u,i} - \bar{R_u})(R_{v,i} - \bar{R_v})}{\sqrt{\sum_{i \in I_u \cap I_v} (R_{u,i} - \bar{R_u})^2 \sum_{i \in I_u \cap I_v} (R_{v,i} - \bar{R_v})^2}}$$

Cosine similarity (between users):

$$Sim(u,v) = \frac{\sum_{i \in I_u \cap I_v} R_{u,i} R_{v,i}}{\sqrt{\sum_{i \in I_u \cap I_v} R_{u,i}^2 \sum_{i \in I_u \cap I_v} R_{v,i}^2}}$$

Collaborative filtering in practice

How does amazon generate their recommendations?



Linden, Smith, & York (2003)

Collaborative filtering in practice

Note: (surprisingly) that we built something pretty useful out of nothing but rating data – we didn't look at any features of the products whatsoever

Collaborative filtering in practice

But: we still have a few problems left to address...

- This is actually kind of slow given a huge enough dataset – if one user purchases one item, this will change the rankings of every other item that was purchased by at least one user in common
- 2. Of no use for **new users** and **new items** ("coldstart" problems
 - 3. Won't necessarily encourage diverse results

CSE 258 — Lecture 7 Web Mining and Recommender Systems

Latent-factor models

So far we've looked at approaches that try to define some definition of user/user and item/item **similarity**

Recommendation then consists of

- Finding an item *i* that a user likes (gives a high rating)
- Recommending items that are similar to it (i.e., items j with a similar rating profile to i)

What we've seen so far are **unsupervised** approaches and whether the work depends highly on whether we chose a "good" notion of similarity

So, can we perform recommendations via **supervised** learning?

e.g. if we can model

 $f(\text{user features}, \text{movie features}) \rightarrow \text{star rating}$

Then recommendation will consist of identifying

 $recommendation(u) = \arg \max_{i \in \text{unseen items}} f(u, i)$

The Netflix prize

In 2006, Netflix created a dataset of **100,000,000** movie ratings Data looked like:

(userID, itemID, time, rating)

The goal was to reduce the (R)MSE at predicting ratings:

$$RMSE(f) = \sqrt{\frac{1}{N} \sum_{u,i,t \in test set} (f(u,i,t) - r_{u,i,t})^2}$$

model's prediction ground-truth

Whoever first manages to reduce the RMSE by **10%** versus Netflix's solution wins **\$1,000,000**

The Netflix prize

This led to **a lot** of research on rating prediction by minimizing the Mean-Squared Error

(it also led to a lawsuit against Netflix, once somebody managed to de-anonymize their data)

We'll look at a few of the main approaches

Let's start with the simplest possible model:

 $f(u,i) = \alpha$

user item

What about the **2nd** simplest model?

$$f(u,i) = \alpha + \beta_u + \beta_i$$
 user item how much does

how much does this user tend to rate things above the mean?

does this item tend to receive higher ratings than others



The optimization problem becomes:

$$\arg\min_{\alpha,\beta} \sum_{u,i} (\alpha + \beta_u + \beta_i - R_{u,i})^2 + \lambda \left[\sum_u \beta_u^2 + \sum_i \beta_i^2 \right]$$

error

regularizer

Jointly convex in \beta_i, \beta_u. Can be solved by iteratively removing the mean and solving for beta

Iterative procedure – repeat the following updates until convergence:

$$\alpha = \frac{\sum_{u,i \in \text{train}} (R_{u,i} - (\beta_u + \beta_i))}{N_{\text{train}}}$$
$$\beta_u = \frac{\sum_{i \in I_u} R_{u,i} - (\alpha + \beta_i)}{\lambda + |I_u|}$$
$$\beta_i = \frac{\sum_{u \in U_i} R_{u,i} - (\alpha + \beta_u)}{\lambda + |U_i|}$$

(exercise: write down derivatives and convince yourself of these update equations!)

Looks good (and actually works surprisingly well), but doesn't solve the basic issue that we started with

f(user features, movie features) =

 $= \langle \phi(\text{user features}), \theta_{\text{user}} \rangle + \langle \phi(\text{movie features}), \theta_{\text{movie}} \rangle$

user predictor

movie predictor

That is, we're **still** fitting a function that treats users and items independently

Dimensionality reduction

We already have some tools that ought to help us, e.g. from week 3:



The "best" rank-K approximation (in terms of the MSE) consists of taking the eigenvectors with the highest eigenvalues

Dimensionality reduction

But! Our matrix of ratings is only partially observed; and it's really big!



SVD is **not defined** for partially observed matrices, and it is **not practical** for matrices with 1Mx1M+ dimensions

Instead, let's solve approximately using gradient descent



Let's write this as: $f(u,i) = \alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i$



Let's write this as: $f(u,i) = \alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i$ Our optimization problem is then



error

regularizer

Problem: this is certainly not convex

Oh well. We'll just solve it approximately

Observation: if we know either the user or the item parameters, the problem becomes easy

$$f(u,i) = \alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i$$

e.g. fix gamma_i – pretend we're fitting parameters for features

This gives rise to a simple (though approximate) solution

objective:

 $\arg\min_{\alpha,\beta,\gamma}\sum_{u,i}(\alpha+\beta_u+\beta_i+\gamma_u\cdot\gamma_i-R_{u,i})^2+\lambda\left[\sum_u\beta_u^2+\sum_i\beta_i^2+\sum_i\|\gamma_i\|_2^2+\sum_u\|\gamma_u\|_2^2\right]$

 $= \arg\min_{\alpha,\beta,\gamma} objective(\alpha,\beta,\gamma)$

1) fix γ_i . Solve $\arg \min_{\alpha,\beta,\gamma_u} objective(\alpha,\beta,\gamma)$

2) fix γ_u . Solve $\arg \min_{\alpha,\beta,\gamma_i} objective(\alpha,\beta,\gamma)$

3,4,5...) repeat until convergence

Each of these subproblems is "easy" – just regularized least-squares, like we've been doing since week 1. This procedure is called **alternating least squares.**

Observation: we went from a method which uses **only** features:

$f(\text{user features}, \text{movie features}) \rightarrow \text{star rating}$



to one which completely ignores them: $\arg \min_{\alpha,\beta,\gamma} \sum_{u,i} (\alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i - R_{u,i})^2 + \lambda \left[\sum_u \beta_u^2 + \sum_i \beta_i^2 + \sum_i \|\gamma_i\|_2^2 + \sum_u \|\gamma_u\|_2^2 \right]$

Should we use features or not? 1) Argument **against** features: Imagine incorporating features into the model like:

$$f(u,i) = \alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i + \langle \phi(u), \theta_u \rangle + \langle \phi(i), \theta_i \rangle$$

which is equivalent to:

$$f(u,i) = \alpha + \beta_u + \beta_i + (\phi(u);\phi(i);\gamma_u) \cdot (\theta_u;\theta_i;\gamma_i)$$

knowns

unknowns

but this has fewer degrees of freedom than a model which replaces the knowns by unknowns:

$$f(u,i) = \alpha + \beta_u + \beta_i + (\gamma'_i;\gamma'_u;\gamma_u) \cdot (\theta_u;\theta_i;\gamma_i)$$

Should we use features or not? 1) Argument **against** features:

So, the addition of features adds **no expressive power** to the model. We **could** have a feature like "is this an action movie?", but if this feature were useful, the model would "discover" a latent dimension corresponding to action movies, and we wouldn't need the feature anyway

In the limit, this argument is valid: as we add more ratings per user, and more ratings per item, the latent-factor model should automatically discover any useful dimensions of variation, so the influence of observed features will disappear

Should we use features or not? 2) Argument **for** features:

But! Sometimes we **don't** have many ratings per user/item

Latent-factor models are next-to-useless if **either** the user or the item was never observed before

$$f(u,i) = \alpha + \beta_u + \beta_i + \gamma_u \cdot \gamma_i$$
reverts to zero if we've never seen the user before (because of the regularizer)

Should we use features or not? 2) Argument **for** features:

This is known as the **cold-start** problem in recommender systems. Features are not useful if we have many observations about users/items, but are useful for **new** users and items.

We also need some way to handle users who are **active**, but don't necessarily rate anything, e.g. through **implicit feedback** Overview & recap

Tonight we've followed the programme below:

- Measuring similarity between users/items for binary prediction (e.g. Jaccard similarity)
- Measuring similarity between users/items for realvalued prediction (e.g. cosine/Pearson similarity)
 - 3. Dimensionality reduction for **real-valued** prediction (latent-factor models)
 - **4. Finally** dimensionality reduction for **binary** prediction

One-class recommendation

How can we use **dimensionality reduction** to predict **binary** outcomes?

- In weeks 1&2 we saw regression and logistic regression. These two approaches use the same type of linear function to predict real-valued and binary outputs
- We can apply an analogous approach to binary recommendation tasks

One-class recommendation

This is referred to as **"one-class"** recommendation

- In weeks 1&2 we saw regression and logistic regression. These two approaches use the same type of linear function to predict real-valued and binary outputs
- We can apply an analogous approach to binary recommendation tasks

One-class recommendation

Suppose we have binary (0/1) observations (e.g. purchases) or positive/negative feedback (thumbs-up/down)



So far, we've been fitting functions of the form

$R\simeq UV^T$

- Let's change this so that we maximize the **difference** in predictions between positive and negative items
- E.g. for a user who likes an item *i* and dislikes an item *j* we want to maximize:

$$\max \ln \sigma (\gamma_u \cdot \gamma_i - \gamma_u \cdot \gamma_j)$$

We can think of this as maximizing the probability of correctly predicting pairwise preferences, i.e.,

$$p(i \text{ is preferred over } j) = \sigma(\gamma_u \cdot \gamma_i - \gamma_u \cdot \gamma_j)$$

As with logistic regression, we can now maximize the likelihood associated with such a model by gradient ascent
In practice it isn't feasible to consider all pairs of positive/negative items, so we proceed by stochastic gradient ascent – i.e., randomly sample a (positive, negative) pair and update the model according to the gradient w.r.t. that pair

Summary

Recap

1. Measuring similarity between users/items for **binary** prediction Jaccard similarity 2. Measuring similarity between users/items for realvalued prediction cosine/Pearson similarity 3. Dimensionality reduction for **real-valued** prediction *latent-factor models* 4. Dimensionality reduction for **binary** prediction one-class recommender systems

Questions?

Further reading:

One-class recommendation: http://goo.gl/08Rh59

Amazon's solution to collaborative filtering at scale: <u>http://www.cs.umd.edu/~samir/498/Amazon-Recommendations.pdf</u> An (expensive) textbook about recommender systems: <u>http://www.springer.com/computer/ai/book/978-0-387-85819-7</u> Cold-start recommendation (e.g.): <u>http://wanlab.poly.edu/recsys12/recsys/p115.pdf</u>